# NAG Toolbox for MATLAB h02bz

# 1 Purpose

h02bz extracts more information associated with the solution of an integer programming problem computed by h02bb.

# 2 Syntax

```
[bl, bu, clamda, istate, ifail] = h02bz(n, m, iwork, rwork, 'liwork',
liwork, 'lrwork', lrwork)
```

# 3 Description

h02bz extracts the following information associated with the solution of an integer programming problem computed by h02bb. The upper and lower bounds used for the solution, the Lagrange-multipliers (costs), and the status of the variables at the solution.

In the branch and bound method employed by h02bb, the arrays **bl** and **bu** are used to impose restrictions on the values of the integer variables in each sub-problem. That is, if the variable  $x_j$  is restricted to take value  $v_j$  in a particular sub-problem, then  $\mathbf{bl}(j) = \mathbf{bu}(j) = v_j$  is set in the sub-problem. Thus, on exit from this function, some of the elements of **bl** and **bu** which correspond to integer variables may contain these imposed values, rather than those originally supplied to h02bb.

#### 4 References

None.

#### 5 Parameters

## 5.1 Compulsory Input Parameters

## 1: n - int32 scalar

This **must** be the same parameter  $\mathbf{n}$  as supplied to h02bb.

Constraint:  $\mathbf{n} > 0$ .

#### 2: m - int32 scalar

This **must** be the same parameter **m** as supplied to h02bb.

Constraint:  $\mathbf{m} \geq 0$ .

#### 3: iwork(liwork) - int32 array

This **must** be the same parameter **iwork** as supplied to h02bb. It is used to pass information from h02bb to h02bz and therefore the contents of this array **must not** be changed before calling h02bz.

### 4: rwork(lrwork) - double array

This **must** be the same parameter **rwork** as supplied to h02bb. It is used to pass information from h02bb to h02bz and therefore the contents of this array **must not** be changed before calling h02bz.

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## 5.2 Optional Input Parameters

#### 1: liwork - int32 scalar

Default: The dimension of the array iwork.

#### 2: lrwork - int32 scalar

Default: The dimension of the array **rwork**.

## 5.3 Input Parameters Omitted from the MATLAB Interface

None.

#### 5.4 Output Parameters

#### 1: bl(n + m) - double array

If h02bb exits with **ifail** = 0, 7 or 9, the values in the array **bl** contain the lower bounds imposed on the integer solution for all the constraints. The first **n** elements contain the lower bounds on the variables, and the next **m** elements contain the lower bounds for the general linear constraints (if any).

#### 2: bu(n + m) - double array

If h02bb exits with **ifail** = 0, 7 or 9, the values in the array **bu** contain the upper bounds imposed on the integer solution for all the constraints. The first **n** elements contain the upper bounds on the variables, and the next **m** elements contain the upper bounds for the general linear constraints (if any).

#### 3: $\operatorname{clamda}(\mathbf{n} + \mathbf{m}) - \operatorname{double} \operatorname{array}$

If h02bb exits with **ifail** = 0, 7 or 9, the values in the array **clamda** contain the values of the Lagrange-multipliers for each constraint with respect to the current working set. The first **n** elements contain the multipliers (reduced costs) for the bound constraints on the variables, and the next **m** elements contain the multipliers (shadow costs) for the general linear constraints (if any).

#### 4: istate(n + m) - int32 array

If h02bb exits with **ifail** = 0, 7 or 9, the values in the array **istate** indicate the status of the constraints in the working set at an integer solution. Otherwise, **istate** indicates the composition of the working set at the final iterate. The significance of each possible value of **istate**(j) is as follows.

istate(i) Meaning

- -2 The constraint violates its lower bound by more than **tolfes** (the feasibility tolerance, see h02bb).
- -1 The constraint violates its upper bound by more than **tolfes**.
- The constraint is satisfied to within **tolfes**, but is not in the working set.
- 1 This inequality constraint is included in the working set at its lower bound.
- 2 This inequality constraint is included in the working set at its upper bound.
- This constraint is included in the working set as an equality. This value of **istate** can occur only when  $\mathbf{bl}(j) = \mathbf{bu}(j)$ .
- This corresponds to an integer solution being declared with  $x_j$  being temporarily fixed at its current value. This value of **istate** can occur only when **ifail** = 0, 7 or 9 on exit from h02bb.

#### 5: ifail – int32 scalar

0 unless the function detects an error (see Section 6).

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# 6 Error Indicators and Warnings

Errors or warnings detected by the function:

```
\begin{aligned} & \text{ifail} = 1 \\ & \text{On entry, } & \textbf{n} \leq 0, \\ & \text{or} & \textbf{m} < 0. \end{aligned}
```

## 7 Accuracy

Not applicable.

## **8** Further Comments

None.

## 9 Example

```
n = int32(6);
m = int32(3);
itmax = int32(0);
msglvl = int32(0);
a = [110, 205, 160,
                       160, 420, 260;
                  13,
                        8,
            32,
        4,
                              4,
                                    14;
            12,
                       285,
                  54,
                             22,
        2,
                                    80];
b1 = [0;
      0;
      0;
      0;
      0;
      0;
      2000;
      55;
      800];
bu = [4;
      3;
      2;
      8;
      2;
      2;
      1e+20;
      1e+20;
     1e+20];
intvar = [int32(1);
          int32(1);
         int32(1);
          int32(1);
          int32(1);
          int32(1)];
cvec = [3;24;13;9;20;19];
maxnod = int32(0);
intfst = int32(0);
toliv = 0;
tolfes = 0;
bigbnd = 1e+20;
x = zeros(6,1);
[itmax, toliv, tolfes, bigbnd, x, objmip, iwork, rwork, ifail] = ...
     hO2bb(itmax, msglvl, a, bl, bu, intvar, cvec, maxnod, intfst, toliv,
tolfes, bigbnd, x);
[bl, bu, clamda, istate, ifail] = h02bz(n, m, iwork, rwork)
```

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```
b1 =
            0
            5
            2
            0
        2000
          55
         800
bu =
   1.0e+20 *
    0.0000
    0.0000
    0.0000
    0.0000
    0.0000
    0.0000
    1.0000
    1.0000
    1.0000
clamda =
    24
    13
     9
    20
    19
     0
     0
istate =
            3
            1
            1
            1
            0
            0
            0
ifail =
            0
```

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